

# Knowing your Lemon before You Dump it

Alessandro Pavan    Jean Tirole



# Motivation

- Situations where decision to “engage” carries information about what is at stake
  - trade
  - partnerships
  - entry
  - marriage
  - ...
- Lemons (Akerlof)
  - *negative inferences*
- Anti-lemons (Spence)
  - *positive inferences*
- **Endogenous information**
  - information acquisition/attention
  - cognition

# This Paper

- Generalized lemons (and anti-lemons)
  - **endogenous information**
- Information choices
  - type of strategic interaction
  - **opponent's beliefs over selected information (expectation conformity)**
    - effect of information on severity of adverse selection
    - effect of friendliness of opponent's reaction on value of information
- **Expectation traps**
- **Disclosure and cognitive style**
- **Welfare and policy implications**
- **Equilibrium analysis and comparative statics**

- **Endogenous info in lemons problem**
  - Dang (2008), Thereze (2022), Lichtig and Weksler (2023)  
→ EC,  $\neq$  bargaining game, timing, CS
- **Payoffs in lemons problem**
  - Levin (2001), Bar-Isaac et al. (2018), Kartik and Zhong (2023)...  
→ incentives analysis
- **Policy in mkts with adverse selection**
  - Philippon and Skreta (2012), Tirole (2012), Dang et al (2017)...  
→ endogenous information
- **Endogenous info in private-value bargaining**
  - Ravid (2020), Ravid, Roesler, and Szentes (2021)...  
→ interdependent payoffs, competitive mkt
- **Expectation conformity**
  - Pavan and Tirole (2022)  
→ different class of games (generalized lemons and anti-lemons)
- **Mandatory disclosure laws**
  - Pavan and Tirole (2023b)  
→ endogenous information

# Plan

- 1 Introduction
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Model

- **Players**

- Leader
- Follower

- **Choices**

- Leader:
  - information structure,  $\rho$  (more below)
  - two actions:
    - **adverse-selection-sensitive**,  $a = 1$  (“engage”)
    - adverse-selection insensitive,  $a = 0$  (“not engage”)
- Follower:
  - reaction,  $r \in \mathbb{R}$

- **State**

- $\omega \sim$  prior  $G$
- mean:  $\omega_0$

- **Payoffs**

- **leader**:  $\delta_L(r, \omega) \equiv u_L(1, r, \omega) - u_L(0, \omega)$ 
  - affine in  $\omega$
  - increasing in  $r$  (higher  $r$ : friendlier reaction)
  - decreasing in  $\omega$
  - benefit of friendlier reaction (weakly) increasing in state:  $\frac{\partial^2 \delta_L}{\partial \omega \partial r} \geq 0$   
(benefit of higher  $r$  largest in states in which  $L$ 's value of engagement lowest)
- **follower**:  $\delta_F(r, \omega) \equiv u_F(1, r, \omega) - u_F(0, \omega)$ 
  - affine in  $\omega$



# Akerlof Example

- Leader: **seller**
  - $u_L(1, r, \omega) = r$  (price)
  - $u_L(0, r, \omega) = \omega$  (asset value)
  - $\delta_L(r, \omega) = r - \omega$
  
- Follower: **competitive buyer**
  - $u_F(0, \omega) = 0$
  - $u_F(1, r, \omega) = \omega + \Delta - r$
  - $\delta_F(r, \omega) = u_F(1, r, \omega)$

- **Information structures:**  $\rho \in \mathbb{R}_+$ 
  - cdf  $G(m; \rho)$  over posterior mean  $m$  (mean-preserving-contraction of  $G$ )
  - $C(\rho)$ : information-acquisition cost

## Definition

Information structures consistent with **MPS order** (mean-preserving spreads) if, for any  $\rho' > \rho$ , any  $m^* \in \mathbb{R}$ ,

$$\int_{-\infty}^{m^*} G(m; \rho') dm \geq \int_{-\infty}^{m^*} G(m; \rho) dm$$

with  $\int_{-\infty}^{+\infty} G(m; \rho') dm = \int_{-\infty}^{+\infty} G(m; \rho) dm = \omega_0$ .

- MPS order and Blackwell informativeness:
  - $G(\cdot; \rho)$  obtained from experiment  $q_\rho : \Omega \rightarrow \Delta(Z)$
  - $G(\cdot; \rho')$  obtained from experiment  $q_{\rho'} : \Omega \rightarrow \Delta(Z)$
  - If  $\rho' > \rho$  means  $q_{\rho'}$  Blackwell more informative than  $q_\rho$ , then

$$G(\cdot; \rho') \succeq_{MPS} G(\cdot; \rho)$$

## Definition

Information structures are **rotations** (or “simple mean-preserving spreads”) if, for any  $\rho$ , there exists rotation point  $m_\rho$  s.t.

- $G(m; \rho)$  **increasing** in  $\rho$  for  $m \leq m_\rho$
- $G(m; \rho)$  **decreasing** in  $\rho$  for  $m \geq m_\rho$

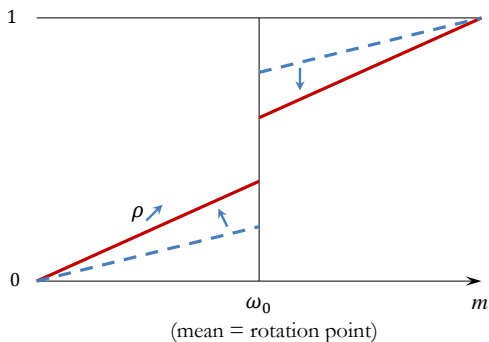
- Diamond and Stiglitz (1974), Johnston and Myatt (2006), Thereze (2022)...

# Rotations Example: Non-directed Search

- $L$  learns state with prob.  $\rho$  (nothing with prob.  $1 - \rho$ )

$$G(m; \rho) = \begin{cases} \rho G(m) & \text{for } m < \omega_0 \\ \rho G(m) + 1 - \rho & \text{for } m \geq \omega_0 \end{cases}$$

- Rotation point: prior mean  $\omega_0$



# Rotations

- Combination of rotations need not be a rotation
- But any MPS can be obtained through sequence of rotations
- Other (notable) examples
  - $G$  Normal and  $s = \omega + \varepsilon$  with  $\varepsilon \sim N(0, \rho^{-1})$
  - Pareto, Exponential, Uniform  $G(\cdot; \rho)$ ...

# Model

- For any  $(\rho, r)$ , leader engages (i.e.,  $a = 1$ ) iff

$$m \leq m^*(r)$$

with

$$\delta_L(r, m^*(r)) = 0$$

- $r(\rho)$ : eq. reaction under information  $\rho$   
(assumed to be unique)

- **Assumption (lemons):**

$$\frac{dr(\rho)}{d\rho} \stackrel{\text{sgn}}{\equiv} \frac{\partial}{\partial \rho} M^-(m^*(r(\rho)); \rho)$$

where

$$M^-(m^*; \rho) \equiv \mathbb{E}_{G(\cdot; \rho)}[m | m \leq m^*]$$

# Akerlof Example

- Engagement threshold:  $m^*(r) = r$
- Equilibrium price  $r(\rho)$ : solution to

$$r = M^-(r; \rho) + \Delta$$

- Lemons:

$$\frac{dr(\rho)}{d\rho} \stackrel{\text{sgn}}{=} \frac{\partial}{\partial \rho} M^-(m^*(r(\rho)); \rho)$$

- always if  $G(m; \rho)/g(m; \rho)$  increasing in  $m$



# Other applications

- Partnerships
- Entry
- Marriage
- OTC mkts
- ...

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# Expectation Conformity

# Effect of information on adverse selection

- $r(\rho)$  : eq. reaction under information  $\rho$

- $M^-(m^*; \rho) \equiv \frac{\int_{-\infty}^{m^*} m dG(m; \rho)}{G(m^*; \rho)}$

## Definition

### Information

- **aggravates adverse selection** if  $\frac{\partial}{\partial \rho} M^-(m^*(r(\rho)); \rho) < 0$
- **alleviates adverse selection** if  $\frac{\partial}{\partial \rho} M^-(m^*(r(\rho)); \rho) > 0$

# Effect of information on adverse selection

$$\frac{\partial}{\partial \rho} M^-(m^*; \rho) \stackrel{\text{sgn}}{\equiv} A(m^*; \rho)$$

where

$$A(m^*; \rho) \equiv [m^* - M^-(m^*; \rho)] G_\rho(m^*; \rho) - \int_{-\infty}^{m^*} G_\rho(m; \rho) dm$$

with  $G_\rho(m; \rho) \equiv \frac{\partial}{\partial \rho} G(m; \rho)$

- Two channels through which information affects AS:
  - **prob. of trade**,  $G_\rho(m^*; \rho)$
  - **dispersion of posterior mean**,  $\int_{-\infty}^{m^*} G_\rho(m; \rho) dm$
- $A(\rho) \equiv A(m^*(r(\rho)); \rho)$ : **adverse-selection effect**

# Effect of unfriendlier reactions on value of information

- $L$ 's payoff under information  $\rho$  and reaction  $r$ :

$$\begin{aligned}\Pi(\rho; r) &\equiv \sup_{a(\cdot)} \left\{ \int_{-\infty}^{+\infty} a(m) \delta_L(r, m) dG(m; \rho) \right\} \\ &= G(m^*(r); \rho) \delta_L(r, M^-(m^*(r); \rho))\end{aligned}$$

- **Benefit of friendlier reaction effect**

- $\rho$ : actual information choice
- $\rho^\dagger$ : anticipated choice (by  $F$ )

$$B(\rho; \rho^\dagger) \equiv -\frac{\partial^2}{\partial \rho \partial r} \Pi(\rho; r(\rho^\dagger))$$

- Starting from  $r(\rho^\dagger)$ , reduction in  $r$ 
  - raises value of information at  $\rho$  if  $B(\rho; \rho^\dagger) > 0$
  - lowers value of information at  $\rho$  if  $B(\rho; \rho^\dagger) < 0$

# Effect of unfriendlier reactions on value of information

$$B(\rho; \rho^\dagger) = -\frac{\partial \delta_L(r, m^*(r(\rho^\dagger)))}{\partial r} G_\rho(m^*(r(\rho^\dagger)); \rho) + \int_{-\infty}^{m^*(r(\rho^\dagger))} \frac{\partial^2 \delta_L(r, m)}{\partial r \partial m} G_\rho(m; \rho) dm$$

- Two channels through which, starting from  $r(\rho^\dagger)$ , reduction in  $r$  affects value of information at  $\rho$ :
  - **prob. of trade**,  $G_\rho(m^*(r(\rho^\dagger)); \rho)$
  - **dispersion of posterior mean**,  $\int_{-\infty}^{m^*(r(\rho^\dagger))} \frac{\partial^2 \delta_L(r, m)}{\partial r \partial m} G_\rho(m; \rho) dm$

# Expectation Conformity

- $L$ 's value function when actual information is  $\rho$  and  $F$  expects information  $\rho^\dagger$ :

$$V_L(\rho; \rho^\dagger) \equiv \Pi(\rho; r(\rho^\dagger))$$

## Definition

**Expectation conformity** holds at  $(\rho, \rho^\dagger)$  iff

$$\frac{\partial^2 V_L(\rho; \rho^\dagger)}{\partial \rho \partial \rho^\dagger} > 0$$



# Key forces...

- $A(\rho^\dagger) \stackrel{\text{sgn}}{=} \frac{\partial}{\partial \rho} M^-(m^*(r(\rho^\dagger))); \rho^\dagger$ : **adverse-selection effect**

- $B(\rho; \rho^\dagger) = -\frac{\partial^2 \Pi(\rho; r(\rho^\dagger))}{\partial \rho \partial r}$ : **benefit-of-friendlier-reactions effect**

# Expectation Conformity

## Proposition

*Assume MPS order.*

*(i) EC at  $(\rho, \rho^\dagger)$  iff  $A(\rho^\dagger)B(\rho; \rho^\dagger) < 0$ .*

*(ii) Information aggravates AS at  $\rho^\dagger$  (i.e.,  $A(\rho^\dagger) < 0$ ) for Uniform, Pareto, Exponential  $G(\cdot; \rho)$ , or, more generally, when  $G_\rho(m^*(r(\rho^\dagger)); \rho^\dagger) < 0$ .*

*(iii) Lower  $r$  raises value for information at  $(\rho, \rho^\dagger)$  (i.e.,  $B(\rho; \rho^\dagger) > 0$ ) if  $G_\rho(m^*(r(\rho^\dagger)); \rho) < 0$ .*

*(iv) Therefore EC at  $(\rho, \rho^\dagger)$  if*

$$\max \left\{ G_\rho(m^*(r(\rho^\dagger)); \rho^\dagger), G_\rho(m^*(r(\rho^\dagger)); \rho) \right\} < 0$$

*(v) Suppose, for any  $m^*$ ,  $M^-(m^*; \rho)$  decreasing in  $\rho$  (e.g., Uniform, Pareto, Exponential) and  $\partial^2 \delta_L(r, m) / \partial r \partial m = 0$  (e.g., Akerlof). Then,  $G_\rho(m^*(r(\rho^\dagger)); \rho) < 0$  NSC for EC at  $(\rho, \rho^\dagger)$ .*

# Non-directed search in Akerlof model

- Akerlof model under non-directed search ( $\rho$ =prob. seller learns state)

$$G(m; \rho) = \begin{cases} \rho G(m) & \text{for } m < \omega_0 \\ \rho G(m) + 1 - \rho & \text{for } m \geq \omega_0 \end{cases}$$

## Corollary

*EC holds at  $(\rho, \rho^\dagger)$  iff  $r(\rho^\dagger) > \omega_0$ , i.e., iff gains from trade  $\Delta$  large.*

# Non-directed search in Akerlof model

- Large  $\Delta$  :  $r(\rho^\dagger) > \omega_0$
- Increase in anticipated information  $\rho^\dagger$ 
  - seller **engages more selectively**,  $G_\rho(m; \rho^\dagger) < 0$
  - **exacerbated AS** (lower  $M^-(m^*(r(\rho^\dagger)); \rho^\dagger)$ )
  - **lower price**
  - higher cost for  $S$  of parting with valuable item
  - **higher value in learning state**

# Non-directed search in Akerlof model

- Small  $\Delta$ :  $r(\rho^\dagger) < \omega_0$
- $S$  engages only when **informed** and  $\omega < r(\rho^\dagger)$
- variations in anticipated information  $\rho^\dagger \rightarrow$  no effect on AS
- No EC

# Gains from Engagement

## Proposition

*Suppose info structures are rotations and  $L$ 's payoff is  $\delta_L(m, r) = \tilde{\delta}_L(m, r) + \theta$ . For all  $(\rho, \rho^\dagger)$ , there exists  $\theta^*(\rho, \rho^\dagger)$  s.t., for all  $\theta \geq \theta^*(\rho, \rho^\dagger)$ , EC holds at  $(\rho, \rho^\dagger)$ .*

- EC more likely when gains from engagement are large.

# Gains from Engagement

- Previous result driven by AS
- Fixing  $r$ ,

$$\frac{\partial^2 \Pi}{\partial \theta \partial \rho} = G_{\rho}(m^*(r, \theta); \rho)$$

- Hence, marginal value of information **decreases with gains from engagement** under suff. condition for EC

$$G_{\rho}(m^*(r(\rho^{\dagger}; \theta), \theta); \rho) < 0$$

- Larger gains  $\rightarrow$  smaller benefit from learning state

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# Expectation Traps

# Expectation Traps

## Proposition

*Suppose  $\rho_1$  and  $\rho_2 > \rho_1$  are eq. levels and information aggravates AS, i.e.,  $A(\rho) < 0$  for all  $\rho \in [\rho_1, \rho_2]$ . Then L better off in low-information equilibrium  $\rho_1$ . Converse true when information alleviates AS, i.e.,  $A(\rho) > 0$ .*

# Expectation Traps: Non-direct search in Akerlof model

- $\rho$ : prob Seller learns state
- $G$  uniform over  $[0, 1]$
- $C(\rho) = \rho^2/20$
- $\Delta = 0.25$
- Eq. conditions

$$r = M^-(r; \rho) + \Delta$$
$$- \int_r^{+\infty} G_\rho(m; \rho) dm = C'(\rho)$$

- Two equilibria:

$$\begin{array}{ll} \rho_1 \approx 0.48 & r_1 \approx 0.69 \\ \rho_2 \approx 0.88 & r_2 \approx 0.58 \end{array}$$

- For any  $m^* > \omega_0$ ,  $G_\rho(m^*; \rho) < 0 \Rightarrow A(\rho) < 0$  (info aggravates AS)
- **Seller better off in low-information eq.**

# Expectation Traps

- **Expectation traps**
  - driven by AS effect
    - friendliness of  $F$ 's reaction decreasing in  $L$ 's information
  - expectation traps emerge **even if information is free**
- Contrast to private values + screening (Ravid et al. 2022)
  - equilibria Pareto ranked
  - eq. payoffs increasing in informativeness of signal

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# Policy Interventions

# Subsidies to Trade

- Welfare (competitive  $F$ ):

$$W \equiv \int_{-\infty}^{m^*} (\delta_L(r, m) + s) dG(m; \rho) - C(\rho) - (1 + \lambda)sG(m^*; \rho)$$

where

- $s$ : subsidy to trade
  - $\lambda$ : cost of public funds (DWL of taxation)
- 
- Subsidy impacts:
    - engagement,  $m^*$
    - friendliness of  $F$ 's reaction,  $r$
    - information,  $\rho$

# Subsidies: Akerlof

- Subsidies optimal in Akerlof model when
  1. Small cost  $\lambda$  of public funds
  2. Information aggravates AS ( $A(\rho) < 0$ )
  3. CS of eq. same as BR: Subsidies reduce information
  
- Proposition 6 (in paper) identifies precise conditions for optimality of subsidies/taxes in generalized lemons/anti-lemons problems.



# Subsidies: Double Dividend

## Corollary

*In Akerlof model, endogeneity of information calls for **larger** subsidy when information reduces prob. of trade.*

- Same condition for EC
- **Double dividend** of subsidy
  - more engagement
  - less information acquisition
- Implication for Gov. asset repurchases programs: **more generous terms**

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# Flexible Information

# Flexible Information

- **Entropy** cost:

- $\rho$  parametrizes MC of entropy reduction (alternatively, capacity)
- $L$  invests in ability to process info (MC or capacity)
- then chooses experiment  $q : \Omega \rightarrow \Delta(Z)$  at cost

$$\frac{1}{\rho} c(I^q)$$

where  $I^q$  is mutual information between  $z$  and  $\omega$

- **Max-slope** cost:

- $\rho$  parametrizes max slope of stochastic choice rule  $\sigma : \Omega \rightarrow [0, 1]$  specifying prob.  $L$  engages
- $L$  chooses  $\rho$  at cost  $C(\rho)$
- then selects experiment  $q : \Omega \rightarrow \Delta(Z)$  and engagement strategy  $a : Z \rightarrow [0, 1]$  among those inducing stochastic choice rule with slope less than  $\rho$

- Key insights similar to those under MPS order

# Equilibrium under Entropy Cost

- Seller's **inner problem** (given  $\rho$ )

$$\int_{\omega} (r - \omega)q(1|\omega)dG(\omega) + \mathbb{E}[\omega] - \frac{I^q}{\rho}$$

where

$$I^q = \int_{\omega} \phi(q(1|\omega))dG(\omega) - \phi(q(1))$$

is entropy reduction, with

$$\phi(q) \equiv q \ln(q) + (1 - q) \ln(1 - q)$$

$$q(1) \equiv \int_{\omega} q(1|\omega)dG(\omega)$$

# Seller's Optimal Signal

- If  $r \leq \underline{r}(\rho)$ , i.e.,

$$\int_{\omega} e^{\rho(r-\omega)} g(\omega) d\omega \leq 1, \quad \int_{\omega} e^{-\rho(r-\omega)} g(\omega) d\omega > 1$$

**never engage**  $\rightarrow q(1) = 0$

- If  $r \geq \bar{r}(\rho)$ , i.e.,

$$\int_{\omega} e^{-\rho(r-\omega)} g(\omega) d\omega \leq 1, \quad \int_{\omega} e^{\rho(r-\omega)} g(\omega) d\omega > 1$$

**always engage**  $\rightarrow q(1) = 1$

- If  $r \in (\underline{r}(\rho), \bar{r}(\rho))$ , i.e., if

$$\int_{\omega} e^{\rho(r-\omega)} g(\omega) d\omega > 1, \quad \int_{\omega} e^{-\rho(r-\omega)} g(\omega) d\omega > 1$$

**interior solution** with information acquisition

- Interior  $q(1|\omega)$  solves functional eq.

$$r - \omega = \frac{1}{\rho} \left[ \ln \left( \frac{q(1|\omega)}{1 - q(1|\omega)} \right) - \ln \left( \frac{q(1)}{1 - q(1)} \right) \right]$$

with

$$q(1) = \int_{\omega} q(1|\omega) dG(\omega)$$

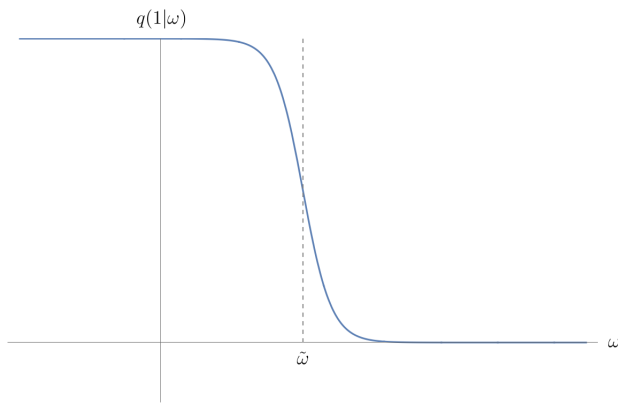
# Seller's Optimal (informative) Signal

- Let  $\tilde{\omega} \in \mathbb{R}$  solve

$$\tilde{\omega} = r + \frac{1}{\rho} \ln \left( \frac{\int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)}{1 - \int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)} \right)$$

- Optimal (interior) signal

$$q(1|\omega) = \frac{1}{1 + e^{\rho(\omega-\tilde{\omega})}}, \quad \tilde{\omega} = r + \frac{1}{\rho} \ln \left( \frac{q(1)}{1 - q(1)} \right)$$





# Equilibrium of Inner Game

Given  $\rho$ , there exists  $\underline{r}(\rho), \bar{r}(\rho)$  s.t. seller's optimal signal

$$q(1|\omega) = \begin{cases} 0 & \forall \omega \text{ if } r \leq \underline{r}(\rho) \\ \frac{1}{1+e^{\rho(\omega-\bar{\omega})}} & \text{if } r \in (\underline{r}(\rho), \bar{r}(\rho)) \\ 1 & \forall \omega \text{ if } r \geq \bar{r}(\rho) \end{cases}$$

Buyer's optimality (given seller's signal  $q$ ):

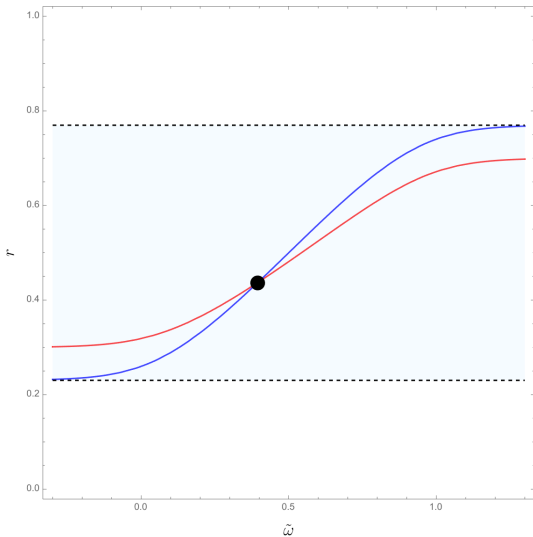
$$r = \int_{\omega} \omega \frac{q(1|\omega)}{\int_{\omega} q(1|\omega) dG(\omega)} dG(\omega) + \Delta$$

# (Interior) Equilibrium of Inner Game

Best-response analysis in  $\mathbb{R}^2$

$$\begin{cases} \tilde{\omega} = r + \frac{1}{\rho} \ln \left( \frac{\int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)}{1 - \int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)} \right) & (\text{seller}) \\ r = \int_{\omega} \omega \frac{\frac{1}{1+e^{\rho(\omega-\tilde{\omega})}}}{\int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)} dG(\omega) + \Delta & (\text{buyer}) \end{cases}$$

# (Interior) Equilibrium of Inner Game



$$\omega \sim U[0, 1], \quad \rho = 10, \quad \Delta = 0.2, \quad r^* \approx 0.44, \quad \tilde{\omega}^* \approx 0.4$$

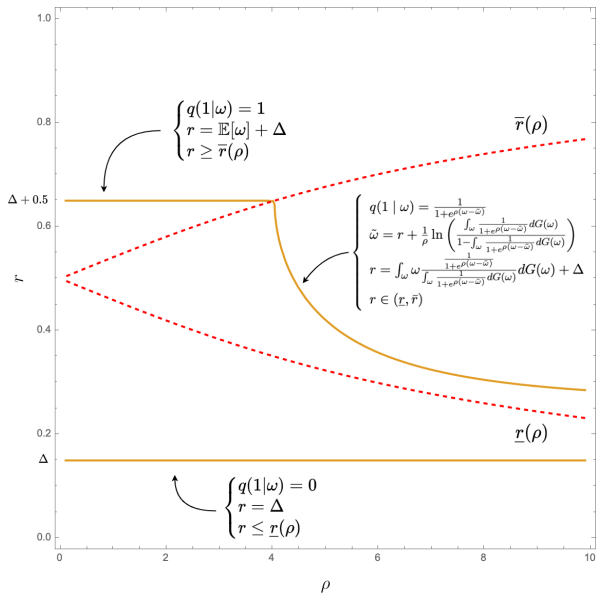
# Multiple Equilibria of Inner Game

- Interior solutions can coexist with corner solutions (with **no information**)
- In case of no engagement, need to specify buyer's *off-path* beliefs
- Following beliefs consistent with most refinements:

$$q^\dagger(1|\omega) = \begin{cases} 1 & \text{if } \omega = 0 \\ 0 & \text{if } \omega \neq 0 \end{cases}$$

- Buyer offers:  $\mathbb{E}[\omega|a = 1; q^\dagger] + \Delta = \Delta$
- If  $\Delta < \underline{r}(\rho)$  seller does not deviate

# Multiple Equilibria of Inner Game



# Outer Game

- Seller first trains herself in processing information
- Endogenous  $\rho$
- $C(\rho)$  : Cost of  $\rho$
- Given  $\rho$ , seller chooses signal flexibly
- Seller's payoff

$$\Pi(r, q; \rho) \equiv \int_{\omega} (r - \omega)q(1|\omega)g(\omega)d\omega + \mathbb{E}[\omega] - \frac{I(q)}{\rho} - C(\rho)$$

# Outer Game: Interior Equilibrium

- Necessary conditions:

$$q^{\rho,r}(1|\omega) = \frac{1}{1+e^{\rho(\omega-\tilde{\omega}(\rho,r))}}, \quad \forall \omega \quad \text{if } r \in (r(\rho), \bar{r}(\rho))$$

$$\tilde{\omega} = r + \frac{1}{\rho} \ln \left( \frac{\int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)}{1 - \int_{\omega} \frac{1}{1+e^{\rho(\omega-\tilde{\omega})}} dG(\omega)} \right)$$

$$\frac{I(q^{\rho,r})}{\rho^2} = C'(\rho)$$

$$r = \int_{\omega} \omega \frac{q^{\rho,r}(1|\omega)}{\int_{\omega} q^{\rho,r}(1|\omega) dG(\omega)} dG(\omega) + \Delta$$

# Outer Game: Numerical Example

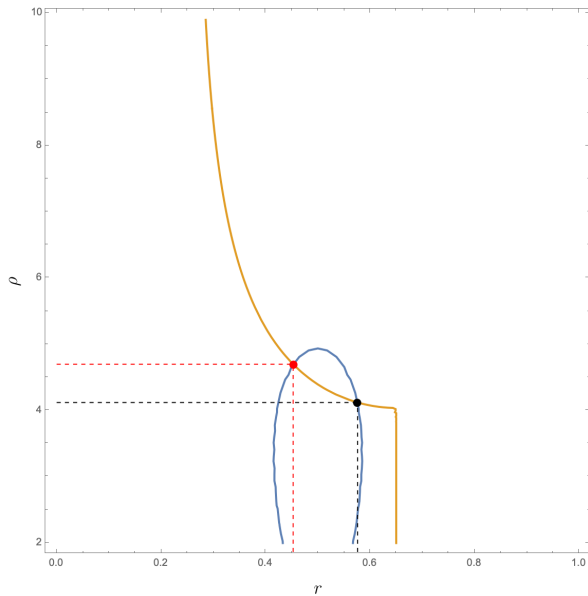
- Assume

$$C(\rho) = \frac{a\rho^2}{2}$$

- with  $a \approx 1.5$  and  $\Delta = 0.15$



# Necessary Conditions: Graphical Analysis

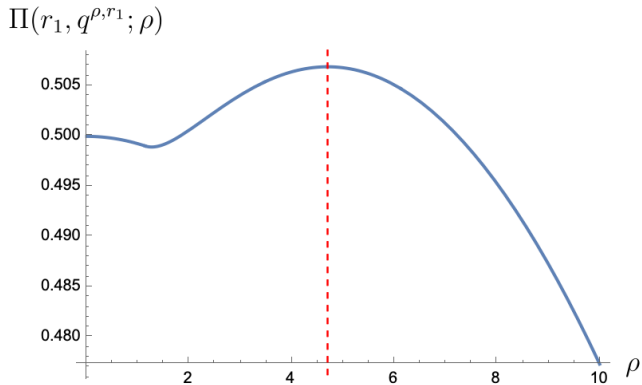


# Candidate (Interior) Equilibria

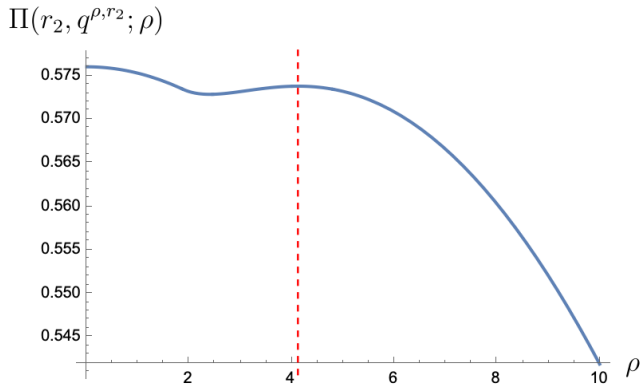
- Two candidate interior equilibria:

$$\rho_1 = 4.7, \quad r_1 \approx 0.45 \quad \text{and} \quad \rho_2 \approx 4.12 \quad r_2 \approx 0.58$$

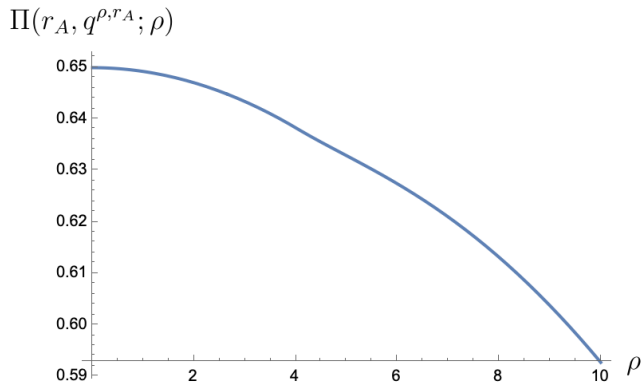
# Sufficiency



# Sufficiency

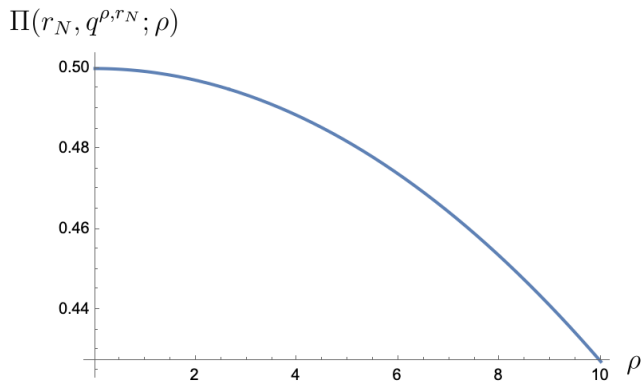


# Corner with Full Engagement



$$\rho = 0, r_A = \int_{\omega} \omega g(\omega) d\omega + \Delta = 0.65$$

# Corner with No Engagement



$$\rho = 0, r_N = \int_{\omega} \omega g(\omega) d\omega + \Delta = 0.15$$

# Multiple Equilibria: Welfare Analysis

- Three equilibria in example with  $\Delta = 0.15$  and  $a \approx 1.5$
- Interior:  $\rho^* \approx 4.7$ ,  $r^* \approx 0.45$ ,  $\Pi(r^*, \rho^*) \approx 0.507$
- Corner with engagement:  $\rho_A = 0$ ,  $r_A = 0.65$ , with  $\Pi(r_A, \rho_A) = 0.65$
- Corner with no engagement:  $\rho_N = 0$ ,  $r_N = 0.15$ , with  $\Pi(r_N, \rho_N) = 0.5$
- Equilibria Pareto ranked:

$$(\rho_N, r_N) \prec (\rho^*, r^*) \prec (\rho_A, r_A)$$

- **Expectation traps**

# Plan

- 1 Introduction
- 2 Model
- 3 Expectation Conformity
- 4 Expectation Traps
- 5 Disclosure and Cognitive Style
- 6 Policy
- 7 Flexible Information
- 8 Anti-lemons
- 9 Conclusions

(Anti-lemons)



# Conclusions

- Endogenous information in mks with adverse selection
- Expectation conformity
  - prob of engagement decreasing in informativemess of signal
  - large gains from interaction
- Expectation traps
- Welfare and policy implications
  - endogeneous info: larger subsidies

# Conclusions

- Ongoing work:
  - bilateral information acquisition
  - public information disclosures
  - ...

THANKS!



# Disclosure

- Suppose  $L$  can prove signal informativeness above  $\hat{\rho}$
- **Hard Information**
- $\hat{\rho}(\rho^*)$ : hard information disclosed in eq. supporting  $\rho^*$
- **Regularity**: Equilibrium supporting  $\rho^*$  is regular if, after disclosing  $\hat{\rho} < \hat{\rho}(\rho^*)$ , informativeness of  $L$ 's signal lower than  $\rho^*$
- Monotone equilibrium selection

## Proposition

*Assume information aggravates AS ( $A(\rho^\dagger) < 0$  for all  $\rho^\dagger$ )*

- *Any pure-strategy eq.  $\rho$  of no-disclosure game also eq. level of disclosure game*
- *Largest and smallest equilibrium levels in regular set of disclosure game also eq. levels of no-disclosure game.*
- Result driven by AS effect
  - disclosing less than eq. level  $\rightarrow$  inconsequential
  - disclosing more  $\rightarrow$  unfriendlier reactions
- Without regularity, eq. in disclosure game supporting  $\rho^* > \sup\{\text{eq. } \rho \text{ no disclosure game}\}$ 
  - sustained by  $F$  expecting large  $\rho$  when  $F$  discloses  $\hat{\rho} < \hat{\rho}(\rho^*)$

- $L$ 's cost  $C(\rho; \xi)$  decreasing in  $\xi$

## Corollary

*Suppose  $L$  can acquire information cheaply ( $\xi_H$ ) or expensively ( $\xi_L$ ) and can disclose only  $\xi_H$  (IQ interpretation) or only  $\xi_L$  (work load). Further assume that, in eq., player  $F$ 's reaction is decreasing in posterior that  $\xi = \xi_H$ . Then  $L$  poses as "information puppy dog", i.e., does not disclose in IQ interpretation and discloses in work load one.*

- $q^{\rho,r}(1|\omega)$ : prob. signal recommends  $a = 1$  at  $\omega$
- $q^{\rho,r}(1)$ : tot prob. signal recommends  $a = 1$
- Entropy:

$$\delta_L(r, \omega) = \frac{1}{\rho} \left[ \ln \left( \frac{q^{\rho,r}(1|\omega)}{1 - q^{\rho,r}(1|\omega)} \right) - \ln \left( \frac{q^{\rho,r}(1)}{1 - q^{\rho,r}(1)} \right) \right]$$

- Max-slope:

$$q^{\rho,r}(1|\omega) = \begin{cases} 1 & \text{if } \omega \leq m^*(r) - \frac{1}{2\rho} \\ \frac{1}{2} - \rho(\omega - m^*(r)) & \text{if } m^*(r) - \frac{1}{2\rho} < \omega \leq m^*(r) + \frac{1}{2\rho} \\ 0 & \text{if } \omega > m^*(r) + \frac{1}{2\rho} \end{cases}$$



## Proposition

Fix  $(\rho, \rho^\dagger)$ .

(i) EC holds at  $(\rho, \rho^\dagger)$  iff  $A(\rho^\dagger)B(\rho; \rho^\dagger) < 0$ .

(ii) Information aggravates AS at  $\rho^\dagger$  if  $q^{\rho, r(\rho^\dagger)}(1|\omega)/q^{\rho, r(\rho^\dagger)}(1)$  increasing in  $\rho$  for  $\omega < m^*(r(\rho^\dagger))$ , decreasing in  $\rho$  for  $\omega > m^*(r(\rho^\dagger))$ , at  $\rho = \rho^\dagger$ .

(iii) Reduction in  $r$  at  $r(\rho^\dagger)$  raises  $L$ 's value of information at  $\rho$  if condition in (ii) holds and  $q^{\rho, r(\rho^\dagger)}(1)$  non-increasing in  $\rho$ .

(iv) Suppose  $M^-(m^*(r(\rho^\dagger)); \rho)$  decreasing in  $\rho$  at  $\rho = \rho^\dagger$  and  $\partial^2 \delta_L(r, m)/\partial r \partial m = 0$  (e.g., Akerlof). Then  $q^{\rho, r(\rho^\dagger)}(1)$  decreasing in  $\rho$  at  $\rho = \rho^\dagger$  NSC for EC at  $(\rho, \rho^\dagger)$ .

**Assumption (anti-lemons).** Friendliness of  $F$ 's reaction to an increase in  $L$ 's information depends **negatively** on impact of  $L$ 's information on adverse selection:

$$\frac{dr(\rho^\dagger)}{d\rho^\dagger} \stackrel{\text{sgn}}{=} -\frac{\partial}{\partial \rho^\dagger} M^-(m^*(r(\rho^\dagger)); \rho^\dagger).$$

# Anti-lemons: Spencian signaling

- $L$ : agent choosing between enrolling in MBA ( $a = 1$ ) or not ( $a = 0$ )
- Cost of enrolling  $\rho$
- Disutility from studying:  $\omega$
- $F$ : representative of competitive set of employers
- Agent's productivity when employed  $\theta = a - b\omega$ ,  $b > 0$
- $r$ : wage offered
- $\delta_L$ :  $r - (\omega + \rho)$
- Engagement threshold:  $m^*(r) = r - \rho$
- Equilibrium  $r(\rho)$ :

$$r = a - bM^-(m^*(r); \rho)$$

## Anti-lemons: Start-up example

- Entrepreneur ( $L$ ) chooses whether to start a business ( $a = 1$ ) at cost  $c_L > 0$
- $1 - \omega$ : probability projects succeeds (delivering 1 unit of cash flows)
- $L$  may need to liquidate prematurely with prob.  $p$  (as in Diamond and Dybvig (1983))
- $r$ : price offered by competitive investors ( $F$ ) in case of liquidation
- $L$ 's payoff from engagement

$$\delta_L = (1 - p)(1 - m) + pr - c_L$$

- Hence,  $L$  engages iff

$$m \leq m^*(r) = \frac{1 - p + pr - c_L}{1 - p}$$

- Value of assets for  $F$ :  $1 - \omega$
- E. price  $r(\rho)$

$$r = 1 - M^-(m^*(r); \rho)$$

## Anti-lemons: Warfare example

- Country  $L$ : potential invader
- $\omega$ : probability country  $F$  wins fight
- $r$ : probability  $F$  surrenders without fighting
- $L$ 's payoff in case of victory: 1;  $L$ 's cost of defeat:  $c_L$

$$\delta_L(r, m) = r + (1 - r)(1 - m - mc_L)$$

- Hence,  $L$  engages iff

$$m \leq m^*(r) = \frac{1}{(1 - r)(1 + c_L)}$$

- $F$ 's payoff from victory: 1;  $F$ 's defeat cost  $c_F$  drawn from cdf  $H$
- Prob.  $r(\rho)$   $F$  surrenders

$$r = 1 - H\left(\frac{M^-(m^*(r); \rho)}{1 - M^-(m^*(r); \rho)}\right)$$

# Anti-lemons: Hermalin (1998)'s leadership model

- $r$ : prob  $F$  joins leader's project
- $\delta_L(r, m) = (1 - m) + r - c_L$
- $1 - m$  : probability project succeeds
- $F$  observes whether  $L$  starts project
- $F$ 's payoff from joining:  $1 - m - c_F$ , with  $c_F$  drawn from cdf  $H$
- Equilibrium  $r(\rho)$

$$r = H(2 - M^-(1 + r - c_L; \rho))$$

## Proposition

Assume MPS order and information aggravates AS at  $\rho^\dagger$  (i.e.,  $A(\rho^\dagger) < 0$ ). EC holds at  $(\rho, \rho^\dagger)$  only if  $G_\rho(m^*(r(\rho^\dagger)); \rho) > 0$ , which, in the case of rotations, happens iff

$$m^*(r(\rho^\dagger)) < m_\rho.$$

Furthermore,  $G_\rho(m^*(r(\rho^\dagger)); \rho) > 0$  necessary and sufficient for EC if  $\partial^2 \delta_L(m, r) / \partial m \partial r = 0$  (e.g., Spence).

- opposite of lemons case